

Original Article

Fusion of Ensemble Classifiers for Handwritten Recognition

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Received: 08 December 2023

Revised: 06 April 2024

Accepted: 11 April 2024

Published: 26 May 2024

Abstract - In the past few years, ensemble techniques were broadly utilized for the task of handwritten recognition rather than single classifiers, which has proved that misclassifications made by classifiers utilizing different feature sets may not certainly overlap. Consequently, integrating classifiers increases the base classifiers' accuracy. In this research work, novel ensemble approaches are presented that are composed of arcing of heterogeneous ensembles and bagged homogeneous classifier ensembles. Then, using accuracy, the classifier performs the classification performances that are assessed using precision. Here, using base classifiers, a classifier ensemble is built, like RBF and SVM. The advantages and feasibility of the presented approaches are proved using the prevailing handwritten recognition dataset. The major novelty of the study relies on three sub processes: pre-processing, categorization and integrating. An extensive array of analogous investigations is completed for a typical database of handwritten recognition. Meanwhile, a comparison study with prior research on the database of handwritten recognition is also revealed. The investigational results reveal that this suggested group approach is reasonable.

Keywords - Arcing, Bagging, Ensemble, Support Vector Machine, Radial Basis Function.

1. Introduction

Handwritten Digit Recognition (HDR) has been effectively enforced in several areas where the precision of acceptance is crucial, like acceptance of the post-mail codes on the cover and account number of the bank or the cash amount inscribed on the chequebook, spontaneous interpretation of zip codes, and much more various approaches are employed in HDR. The collection of categorizers has been broadly employed in minimizing model ambiguity and enhancing simplification accomplishment. Establishing methods for producing candidate group representatives is a significant way of collecting categorizers study. It has been shown that a virtuous group is one in which the particular categorizers in the group are both precise and make their mistakes on diverse fragments in the input space. The remaining of the research is outlined as mentioned below. Section 2 deliberates the prior research completed. Section 3 defines the new method suggested in this article. Section 4 describes the categorization accomplishment along with analyzation procedures—Sections 5 and 6 pact with the outcomes and inference.

2. Related Work

A huge number of exploring was performed in the HDR field where several methods are protected, and there yet exists several unprotected ones. S M Shamim et al. (2018) [15]

introduced an approach to non-computerized HDR founded on diverse ML methods. The major objective of this study is to ensure competent and dependable approaches for analyzation of HDR.

Various ML procedures called Naïve Bayes, SVM, Bayes Net, Multilayer Perceptron, Random Tree, Random Forest, and J48 have been employed for the analysis of figures by implementing WEKA.

M.MerlineMagrina et al. (2019) [9] are employed to analyze antique Tamil Writing in gravels. OCR segment of application is Ensemble Learning is majorly concentrated in this research.

SavitaAhlawat et al. (2020) [13] suggested a study to discover several design choices such as stride size, kernel size, number of layers, receptive field, dilution, and padding for CNN-founded HDR.

Ayush Kumar Agrawal et al. (2021) [2] contemplated a custom CNN prototype to accurately analyze the HDR by implementing a diverse set of maximisers. The actions of the introduced model have been investigated on the public MNIST database. The outcomes demonstrate that the efficiency of the prototype exceeds various modern methods in the presented area.



Mamatarani Das et al. (2022) [8] demonstrated the accomplishment of five diverse ML prototypes that implement a complex NN in finding HDR digits in response to the HDR database that is extended and operated by implementing various additional methods to make disparity and surge the capacity of the info in the specified database. Syed Sohail Ahmed et al. (2023) [17] attempted to overwhelm the above-mentioned restrictions by presenting Deep Learning (DL) based models such as EfficientDet-D4 for many classifications. Firstly, the input imageries are explained to precisely illustrate the Region of Interest (ROI). In the subsequent stage, these imageries are employed in order to train the EfficientNet-B4-based EfficientDet-D4 technique to identify and classify the numbers into their respective classes from 0 to 9.

Based on the prior research, a mixed system is suggested by implementing RBF and SVM and the efficiency of the suggested Bagged SVM (BSVM), Bagged RBF (BRBF), and RBF-SVM fusion structure is analyzed by carrying out various trials on US zip code database. The accomplishment of the suggested BSVM, BRBF, and RBF-SVM fusion categorizers are investigated in associative with discrete SVM and RBF categorizers. In addition, heterogeneous prototypes reveal improved outcomes than homogeneous prototypes and associations with the above research on a typical database of HDR are also itemized.

3. Suggested Model

3.1. Preprocessing

In the process of database pre-processing, transformation and cleaning are executed. Cleaning indicates the removal of unnecessary tags and filling up the missed values in the datasets. Transformation indicates the translating task of the complete dataset into the preferred form (it is the conversion task of numeric values into the character data type).

3.2. State of Art Models

3.2.1. RBF

A radial basis function, RBF, $\phi(x)$ denotes a function with esteem to the basis or a definite point c , i.e., $\phi(x)=f(\|x-c\|)$ where the norm is generally the Euclidean but can be other kind of measure. To alter the distance from a certain place, RBF utilizes RBF for activation. The system control, time-series prediction, and classification are used by RBF for functional approximation. RBF was utilized for classifying records in non-linear mode and compared entering records with trained datasets. The weighted linear superposition is the manufacture of the RBF NN. In the RBF prototype, the Gaussian-basis procedure is the frequently used basis function [5].

3.2.2. SVM

This is developed by [11] and broadly used to train SVM. The well-known calculation of a hyperplane is $w \cdot x + b = 0$. While, w denotes the vector normal to hyperplane and b refers

to an offset. If the value of $w \cdot x + b > 0$, then it indicates the positive point, or else it is a negative point. SMO is a simple solution to solving a Quadratic Programming (QP) problematic issue that arises in the exercise process of SVM. SMO splits the huge QP issue into a sequence of minute sub-issues. Such minor sub-issues are methodically resolved, stopping the implementation of time-consuming arithmetical QP maximization as an inner iteration. It was a rapid process for sparse datasets and linear SVM and comparatively faster than the chunking method. The retention looked for SMO is linear in the exercise datascope, allowing SMO to deal with huge exercise sets. It scales amongst quadratic and linear in the exercise set scope for various trial issues.

3.3. Homogeneous Group Classification Model

3.3.1. BRBF and BSVM Classification Model

Presented a collection of D , of d tuples, bagging [4]. For iterations i ($i = 1, 2, \dots, k$), a trained dataset, D_i , of d tuples undergoes sampling by substituting the initial set of tuples, D . From the presented training database, D repeatedly, the bootstrap example, D_i , made by D trial with reinstatement. All examples in the exercise set D were found to be repetitive or not at all in any specific replicate exercise dataset D_i . For all training sets, the D_i A categorizer prototype, M_i , is studied. To categorize a mysterious tuple, X , All categorizers, M_i , returned its class anticipation, which may be counted as a single vote. The SVM and bagged RBF, M^* , will count the amount of votes and allot the session with the maximum amount of votes to X .

Algorithm: Pseudocode of RBF and SVM group classification model bagging

Input:

- D : collection of d tuples.
- $k = 2$, classifier count in the ensembling process, and the amount of classification prototypes in the group.
- Baseline Categorizer (RBF, SVM)

Output: BRBF and BSVM, M^*

Method:

- (1) for $i = 1$ to k do // generate k methods
- (2) Generate bootstrap samples, D_i , via substituting specimen D from the provided exercise data D recurrently. Every instance in the specific exercise data D might occur several iterations or be absent in a specific replicating exercise dataset D_i
- (3) Utilize D_i for model derivation, M_i ;
- (4) Classification of examples d in train dataset D_i and weight initialization, W_i for the prototype, M_i , depending upon the accuracy of the fraction of properly categorized samples in exercise dataset D_i .
- (5) Endfor

For using BRBF and BSVM approaches on the tuple, X:

1. if categorization then
2. consider every one of the k methods for classifying X and save a major number of votes;
3. if forecasting then
4. consider every one of the k methods for predicting a value for X and offer regular outcomes;

3. if forecasting then
4. consider every one of the k methods for predicting a value for X and offer regular outcomes;

3.4. Heterogeneous Group Classification Model

3.4.1. RBF-SVM Fusion Model

Provided a set D of d tuples, the arcing [3] study is mentioned below. For repetition, i (i =1, 2,.....k), an exercise set, D_i , of d tuples is trialed with substitution from the initials et of tuples, D. Few samples from the database D will ensure more than once in the exercise database D_i .

The samples that did not qualify for the exercise database concluded creating the trial database. Then, a categorizer prototype, M_i , is calculated for every exercise sampled from the exercise database D_i . A categorizer prototype, M_i , is calculated for every exercise set, D_i .

The fusion categorizer M^* and RBF-SVM sums the number of votes and allocates the session with the majority votes to X. For categorizing an unidentified tuple, X, all categorizers, M_i , return its class anticipation that amounts to a single vote.

Algorithm: Pseudocode of Fusion RBF-SVM by Arcing Classification Model

Input:

- D: collection of d tuples.
- $k = 2$, classifier count in the ensembling process
- Baseline Classifier (RBF, SVM)

Output: Fusion SVM-RBF model, M^* .

Procedure:

1. For i = 1 to k do // Generate k methods
2. Generate exercise data, D_i , via sampling D with substitution.
3. Utilize D_i for model derivation, M_i
4. Classification of examples d in train dataset D_i and weight initialization, W_i for the approach, M_i , depending upon the accuracy of the fraction of properly categorized samples in exercise dataset D_i .
5. endfor

For using a fusion prototype on the tuple, X:

1. if categorization then
2. consider every one of the k methods for classifying X and save the major number of votes;

4. Experimental Setup

The data is partitioned into subsets trained, and another subset is used to calculate the performance of the prototype using the Cross-validation technique. The performance of any algorithm can be described using accuracy with which positive and negative instances can be predicted properly by an algorithm.

5. Experimental Validation

5.1. Characteristics of US Zip Code Database

Table 1. Properties of signature verification database

Dataset	Instance	Attribute
US Zip code	4253	16

5.2. Comparative Analysis of the Homogeneous and Heterogeneous Ensembles

Suggested group precisions are evaluated to investigate the accomplishment of the heterogeneous and homogeneous prototypes.

In this work, novel combined categorization prototypes are presented for homogeneous groups involving bagging, and the performance contrasts are established utilizing a standard database of handwritten recognition with respect to precision. Here, the suggested groups incorporate aspects of subsequent single categorizers.

Likewise, a novel hybrid RBF-SVM group prototype is constructed with arcing, and the precision is calculated. Both prototypes are associated with base categorizers in regard to precision for the US zip code database, as provided in Table 2.

In accordance with Figure 1, a huge enhancement of precision is detected for suggested fusion techniques than single base categorizers, and heterogeneous collections display greater accomplishment related to homogeneous methods.

Table 2. Comparative analysis of the Homogeneous and Heterogeneous Group Classifications for HDR

Database	Classifier	Classification Accuracy%
U.S Zip Code	RBF	86.46
	BRBF	97.74
	SVM	93.98
	BSVM	95.45
	Hybrid RBF-SVM	99.13

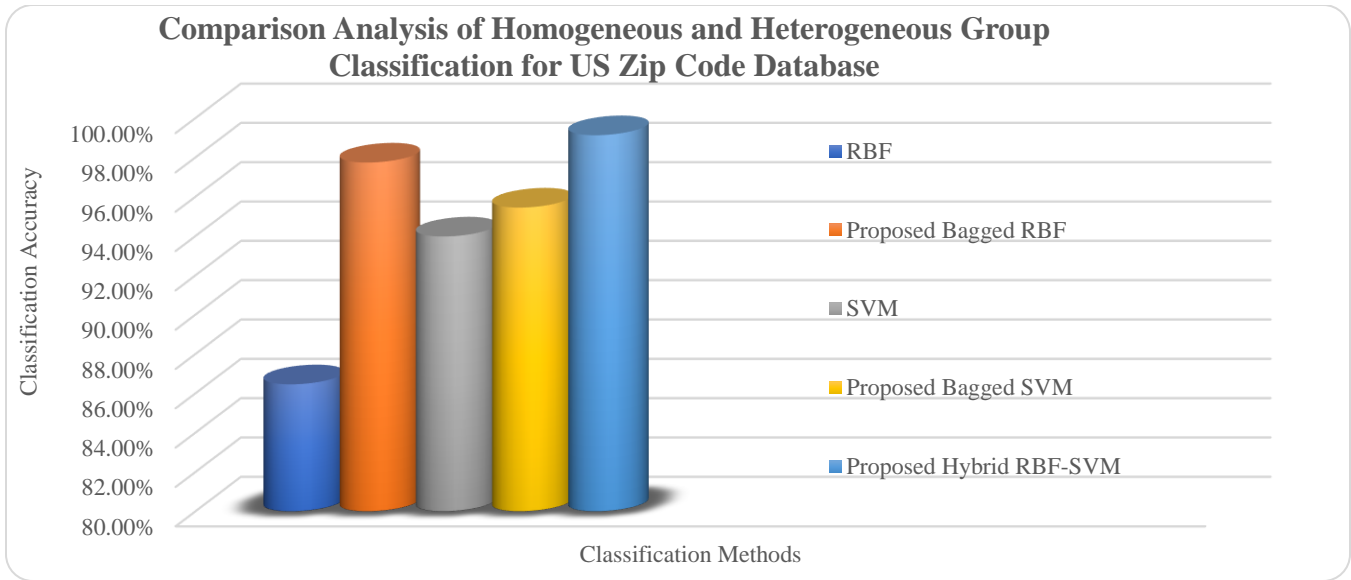


Fig. 1 Precision for Homogeneous as well as heterogeneous ensemble classifications in the US zip code database

5.3. Comparison Analysis with Previous Research

It is observed in Table 3 that greater accuracy is performed with heterogeneous and homogeneous prototypes related to previous studies on the HDR. Moreover, the suggested categorizer proves to demonstrate demographically crucial accomplishment than modern methods. The homogeneous prototypes have been identified to accomplish outstanding improvement of categorization precision when related to associating discrete categorizers at the cost of large training time. This is because the homogeneous prototypes

combine the complementary features of the base classifiers. In contrast, the use of simpler base learners will probably not give immediate practical performance results but could lead to further useful theoretic insights. The heterogeneous prototype displays a greater precision fraction when related to discrete categorizers. The combination of weak and strong base learners for ensembles has the advantage of using the logic of both sides and delivering the best solution to present a data-intensive calculating process.

Table 3. Experimentation Outcomes of Homogeneous and Heterogeneous Group Classification for US Zip Code Database

Methods	Precision Claimed
RBF	86.46%
SVM	93.98%
Homogeneous Group Classifications	
Suggested Bagged RBF	97.74%
Guido Bologna et al., 2017 [7]	94.56%
Soumya Ukil et al. 2018 [16]	94.73%
Amjad Ali Al-Jourishi et al. 2020 [1]	97.60%
Mir Moynuddin Ahmed Shibly et al., 2021 [10]	93.55%
Waleed Albattah et al., 2022 [18]	97.10%
Suggested Bagged SVM	95.45%
Yildiz Aydin et al. 2017 [20]	91.00%
RandaElanwar et al. 2018 [12]	95.18%
K V Greeshma et al., 2020 [6]	91.59%
Yasir Babiker Hamdan et al., 2021 [19]	88.00%
Waleed Albattah et al., 2022 [18]	93.90%
Heterogeneous Group Classifications	
Suggested Hybrid RBF-SVM	99.13%
Guido Bologna et al., 2017 [7]	98.39%
RandaElanwar et al. 2018 [12]	97.30%
Amjad Ali Al-Jourishi et al. 2020 [1]	97.51%
Mir Moynuddin Ahmed Shibly et al., 2021 [10]	98.68%
Shajun Nisha et al., 2022 [14]	98.66%

6. Conclusion

In this research, a new method of associating the categorization prototypes concerning homogeneous groups with bagging is employed by implementing US zip code information. The categorizer accomplishment is described with precision. Also, the suggested groups incorporate aspects of subsequent single categorizers. Similarly, a new fusion heterogeneous RBF-SVM group prototype is built, and the precision is calculated.

The below comments are exposed from the outcomes.

- ❖ Amongst the standalone categories employed, SVM describes crucially greater accomplishment insignificant features of precision.
- ❖ The bagged prototypes have been identified to accomplish outstanding improvement of categorization precision when related to associating discrete categorizers.
- ❖ RBF-SVM prototype displays greater precision fraction when related to discrete categorizers.

- ❖ The fusion prototypes demonstrate crucially huge precision outcomes than collective prototypes on the US zip code database.
- ❖ The demographic importance is also found to be huge for the suggested categorizers rather than base categorizers.
- ❖ Outcomes also specify the heterogeneous and homogeneous prototypes exceeding prior work on the HDR database.
- ❖ The constraint for the group is difficult to study, and any wrongful selection can pave the way to less forecasting precision than a discrete prototype.
- ❖ Developing and employing greatly literal categorizers precisely for the US zip code database will be the upcoming study.

Acknowledgments

The author recognizes Annamalai University authorities for their esteemed assistance in completing this study.

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