

Computer Simulation of The Heat Load Scrutiny For Best Use of Cupola Furnace

Shadrack Mathew Uzoma¹, Tobinson A. Briggs²

^{1,2}Mechanical Engineering Department, University of Port Harcourt
Nigeria

Abstract : The cupola is a cylindrical steel shell that handles over 90% of iron from a blast furnace in the conversion process to iron castings and steel manufacture. Operational efficiencies of cupola had been tagged to fluctuate between 30% and 50%. The thermal performance limits were mainly experimental. Hence the need for validation employing computer simulation approach. In this work, the cupola or cupolette was designed to handle one ton of charge per heat per day. Mathematical models had been developed by the researchers to validate the stipulation; in there titled “Heat Load Analysis for Optimal Use of Cupola Furnace In Iron Castings and Steel Manufacture” [10]. Alumina (Al_2O_3) refractory was employed as the lining for the furnace. The refractory and shell thicknesses were varied within a reasonable range. The results of the cupola computer simulation confirmed the maximum thermal efficiency of 19.81% when the thickness of the refractory material is 115mm, and steel shell thickness is 5mm. It is worthy to note that the employment of cupola of larger sizes, also simulating the refractory lining of different materials, could tremendously boost the performance of the cupola furnace.

Keywords: Cupola, Blast furnace, Iron castings and steel manufacture, Operational efficiency, Alumina Refractory, computer simulation, and shell thicknesses.

I. INTRODUCTION

A cupola is essentially a cylindrical steel shell employed in the smelting of scrap metals, and more or less 90% of pig iron used in the production of iron castings [1]. The operating efficiency of the cupola is very paramount. The available heating space is extremely affected by the thermal performance of the cupola furnace. The design and construction of cupola ensure maximum heat conservation and recovery in the workspace, which is a critical factor in its performance[10]. The performance efficiency improvement of the furnaces, as well as the cupola, the optimization of furnace lining thickness by determination of the critical radius of insulation and experimenting with different grades of refractory lining materials, should be considered [2,3,4,5,6]. In this research, only alumina refractory was used in the computational approach to determining the cupola thermal performance and other related parameters. A cupola could melt 15 tons of pig iron

per hour, while a cupolette could handle one ton of charge, comprising of pig iron, scrap metal and steel, coke, and flux per heat per day [7, 10]. The available heat in the heating space should be of stringent consideration. The heat is the determinant factor for the operational, thermal, or performance efficiency of the cupola.

The approach to investigating the thermal efficiency of the cupola is through the development of mathematical models that balance the heat load in the different zones of the cupola. Preference would also be placed on the refractory material thickness viz-a-viz the thickness of the steel shell of the cupola.

II. Research Significance

The determination of cupola thermal performance largely has been inclined to design, construction, and experimental procedures. This research investigates the thermal performance concept of cupola through mathematical models development and computer simulation.

III. Relevant Mathematical models

Equation 1 to 25 was re-invoke from the mathematic model used by Briggs and Uzoma in their previous work on heat load analysis for a cupola furnace. The rate of heat transfer through the steel shell given as [10]:

$$\dot{q}_{rm} = -\frac{2\pi k_2 L}{\ln \frac{r_2}{r_1}} (T_2 - T_1) = -\frac{T_2 - T_1}{\frac{n_{r23}}{r_1} \frac{2\pi k_2 L}{2\pi k_2 L}} \quad (1)$$

Heat transfer through the refractory material given as :

$$\dot{q}_{rm} = -\frac{2\pi k_2 L}{\ln \frac{r_2}{r_1}} (T_2 - T_1) = -\frac{T_2 - T_1}{\frac{n_{r23}}{r_1} \frac{2\pi k_2 L}{2\pi k_2 L}} \quad (2)$$

Heat transfer by convection to the internal surface of the furnace lining could be represented as:

$$\hat{q}_{mr} = -h_m (2\pi r_1 L) (T_1 - T_m) = -\frac{(T_1 - T_m)}{\frac{1}{2\pi r_1 h_m L}} \quad (3)$$

The heat transfer rate from the surface of the steel shell to the surroundings by convection could express as :

$$\hat{q}_{sa} = -h_a (2\pi r_3 L) (T_a - T_3) = -\frac{(T_a - T_3)}{\frac{1}{2\pi r_3 h_a L}} \quad (4)$$

Rearranging equations 1, 2, 3, and 4, and the expression for the inter-boundaries temperatures T_1 , T_2 , and T_3 are derived :

$$r_1 h_m T_1 + r_3 h_a T_3 = r_1 h_m T_m + r_3 h_a T_a \quad (5)$$

$$k_1 \ln(r_3/r_2)T_1 - \left[k_1 \ln\left(\frac{r_3}{r_2}\right)k_2 \ln\left(\frac{r_2}{r_1}\right) \right] T_2 + k_2 \ln\left(\frac{r_2}{r_1}\right) T_3 = 0 \quad (6)$$

$$r_1 h_m \ln(r_3/r_2)T_1 + k_2 T_2 - k_2 T_3 = r_1 h_m \ln(r_3/r_2) T_m \quad (7)$$

The rate of heat flow from the surface of the steel shell to the surrounding air given as [10] :

$$\dot{q}_r = -\frac{(T_m - T_a)}{2\pi r_1 h_m L + \frac{1}{2\pi k_1 L} \ln\left(\frac{r_2}{r_1}\right) + \frac{1}{2\pi k_2 L} \ln\left(\frac{r_3}{r_2}\right)} = -\frac{2\pi L(T_m - T_a)}{\frac{1}{r_1 h_m} + \frac{1}{k_1} \ln\left(\frac{r_2}{r_1}\right) + \frac{1}{k_2} \ln\left(\frac{r_3}{r_2}\right) + \frac{1}{r_3 h_a}} \quad (8)$$

The heat load of the system per day represented as :

$$Q_r = Q_{iron} + Q_{coke} + Q_{flux} - Q_{RZ} + Q_{HOTAIR} - Q_{exhaust} \\ = (m_{c_p} \Delta T)_{iron} + (m_{c_p} \Delta T)_{coke} + (m_{c_p} \Delta T)_{flux} + \rho_a \dot{V}_a C_{pair} \Delta T_{hotair} - \rho_{air} \dot{V}_a C_{pair} \Delta T_{exhaust} \quad (9)$$

A cupola or cupolette with the capacity of refining one ton of iron per heat per day has an iron-coke – flux ratio of 0.906: 0.091: 0.00362. On the mass basis of one ton, the ratio in kilogram becomes 906: 91: 3.62 [8, 10]. The heat load expression in Equation 13 can be re-expressed as :

$$Q_r = (906 \times C_p \Delta T)_{iron} + (91 \times C_p \Delta T)_{coke} + (3.62 \times C_p \Delta T)_{flux} + \rho_a \dot{V}_a \Delta T_{hotair} - \rho_{air} \dot{V}_a \Delta T_{exhaust} \quad (10)$$

different zones of the cupola being, the stack, the preheat zone, melting zone, reducing zone, combustion zone, and the well can be represented as H1, H2, H3, H4, H5, and H6. The dimensional relationships and temperature distribution in the different zones, while the overall cupola height, H given as six meters is represented as follows [10] :

$$STACK, 0 \leq H1 \leq 1m, Temperature = 600^\circ C$$

$$PREHEATZONE 1m \leq H2 \leq 4m, " = 110^\circ C$$

$$MELTINGZONE 4m \leq H3 \leq 5m, " = 1600^\circ C$$

$$REDUCINGZONE 5m \leq H4 \leq 5.2m, " = 1200^\circ C$$

$$COMBUSTIONZONE 5.2m \leq H5 \leq 5.6m, " = 1850^\circ C$$

$$WELL 5.6 \leq H6 \leq 6m, " = 1500^\circ C$$

The reactions in the reducing zone are endothermic.

The average temperatures of the zones over their interfacial boundaries are given as below [10] :

$$\left[\begin{array}{l} \Delta T_{H1} = [400 - 28] = 380^\circ C \\ \Delta T_{H2} = [1100 - 28] = 1078^\circ C \\ \Delta T_{H3} = [1600 - 28] = 1578^\circ C \\ \Delta T_{H4} = [1850 - 28] = 1822^\circ C \\ \Delta T_{H5} = [1500 - 28] = 1472^\circ C \end{array} \right] \quad (11)$$

Performing heat balance at the different zones :

(i) Stack zone

$$Q_{SZ} = \rho_{air} V_{rs} C_{pair} \Delta T_{H1} \quad (12)$$

(ii) Preheat zone

$$\dot{Q}_{SZ} = (906 \times C_{piron} + 91 \times C_{pcoke} + 3.62 \times C_{pflux}) \Delta T_{H2} \quad (13)$$

(iii) Melting zone

$$Q_{PHZ} = (906 \times C_{piron} + 91 \times C_{pcoke} + 3.62 \times C_{pflux}) \Delta T_{H3} \quad (14)$$

(iv) Reducing zone

$$Q_{RZ} = (906 \times C_{piron} + 91 \times C_{pcoke} + 3.62 \times C_{pflux}) \Delta T_{H4} \quad (15)$$

(iv) Combustion zone

$$Q_{CZ} = (906 \times C_{piron} + 91 \times C_{pcoke} + 3.62 \times C_{pflux}) \Delta T_{H4} \quad (16)$$

The net amount of heat to melt a ton of the charge expressed as

$$Q_{NET} = Q_{PHZ} + Q_{MZ} + Q_{CZ} - Q_{RZ} + Q_{HOTAIR} - Q_{EXHAUST} \quad (17)$$

If C_{coal} (J/kg) is the calorific value of coal and the mass of coal consumed is m (kg), then the amount of heat provided for smelting operation could be given as :

$$\dot{Q}_{coal} = \dot{m} C_{coal} \quad (18)$$

The heat content of the hot air expressed as:

$$\dot{Q}_{air} = \rho_{air} \dot{V}_{air} C_{pair} \Delta T_{air} \quad (19)$$

Where,

$$\Delta T_{air} = T_{blast} - T_{exhaust} \quad (20)$$

The heat of formation of carbon dioxide is this expressed as:

$$C(s) + O_2(g) \rightarrow CO_2(g) \Delta H_{25^\circ C}^0 = -\frac{94050 \text{ Cal}}{\text{mole}} \quad (21)$$

Heat evolution due to the oxidation of iron to the highest oxidation state being Fe_2O_3 given as:

$$\Delta H_{Fe_2O_3}^0 = -196500 \text{ cal/mole of } Fe_2O_3 \quad (22)$$

The heat of formation of MnO per mole gave as:

$$\Delta H_{MnO}^0 = -35209 \text{ Cal/mole} \quad (23)$$

The heat of formation of SiO_2 per mole expressed as :

$$\Delta H_{SiO_2}^0 = -88618 \text{ cal/mole} \quad (24)$$

Based on the over-riding stipulated conditions, the thermodynamic efficiency of a cupola furnace system expressed as :

$$\eta_{th} = \frac{\text{Heat utilized in preheating + melting + superheating}}{\text{Heat due to calorific value of coke + Heat evolved due to oxidation of C, Fe, Si and Mn} + \text{Heat content of air blast} - \text{Heat utilized in the reducing zone} - \text{Exhaust heat}} \\ = \frac{Q_{PHZ} + Q_{MZ} + Q_{CZ}}{Q_{coke} + Q_{oxi} + Q_{hotair} - Q_{RZ} - Q_{exhaust}} \quad (25)$$

IV. INPUT PARAMETERS TO THE ALGORITHMIC CODING

Cupola or cupolette iron : coke : flux ratio = 0.906 : 0.091 : 0.0362

Considering one ton of charge the iron : coke : flux ratio in kilogram = 906 : 91 : 3.62

The charge constituents or compositions are depicted as follows :

		%		
Properties of constituents				
C	Si	Mn	P	S
15%	Pig Iron	No 1	3.5	3.5
0.7	0.17	0.016		
20%	Pig Iron	N0 2	3.5	3.0
0.65	0.11	0.030		
30%	New Scrap		3.4	2.3
0.5	0.2	0.035		
35%	returns (gate, risers, etc)		3.3	2.5
0.65	0.16	0.035		

Iron Loss Due to Oxidation Reaction

Iron loss due to oxidation reaction is assumed to equal to the carbon that is absorbed in the process of refinement, and it is express as :

(Weight of metal charge)x(Proportion or fraction of constituent in the charge)x(Fraction of element in the charge).

% of carbon in the final analysis :
 Pig iron No 1 : $906 \times (15/100) \times 0.035 = 4.7565 \text{kg}$
 Pig iron No 2 : $906 \times 0.2 \times 0.035 = 6.342 \text{kg}$
 New scrap : $906 \times 0.3 \times 0.034 = 9.2412 \text{kg}$
 Returns : $906 \times 0.35 \times 0.033 = 10.4643 \text{kg}$
 Total = 30.804kg

% of carbon in the final analysis = $(30.804/1000) \times 100 = 3.0804\%$
 Iron loss to oxidation reaction = $3.0804\% = (3.0804/100) \times 906 = 27.9084 \text{kg}$
 Silicon loss due to oxidation Silicon loss due to oxidation is about 10%
 Pig iron No 1 : $906 \times 0.15 \times 0.025 = 3.3975 \text{kg}$
 Pig iron No 2 : $906 \times 0.2 \times 0.03 = 5.436 \text{kg}$
 New scrap : $906 \times 0.3 \times 0.023 = 6.2514 \text{kg}$
 Returns : $906 \times 0.35 \times 0.025 = 7.9275 \text{kg}$
 Total = 23.0124kg

Silicon loss = $23.0124 \times (10/100) = 2.30124 \text{kg}$
 Manganese loss due to oxidation Manganese suffers loss of about 15%
 Pig iron No 1 : $906 \times 0.15 \times 0.007 = 0.9513 \text{kg}$
 Pig iron No 2 : $906 \times 0.2 \times 0.0065 = 1.1778 \text{kg}$
 New scrap : $906 \times 0.3 \times 0.005 = 1.359 \text{kg}$
 Returns : $906 \times 0.35 \times 0.0065 = 2.06115 \text{kg}$
 Total = 5.54925kg

Manganese loss = $5.54925 \times (15/100) = 0.83239 \text{kg}$

Carbon loss due to oxidation to carbon dioxide
 Volumetric analysis of the exhaust gases:
 $\text{CO}_2 : \text{CO} : \text{N}_2 = 12\% : 12\% : 76\%$
 $\text{CO}_2 = 1 \text{ mole C} + 2 \text{ moles O} = 12 + 32 = 44 \text{kg}$
 % of C oxidized = $(12/44) \times 12\% = 3.273\%$
 Assuming the amount of coke in the combustion zone of the cupola to initiate combustion is 3kg;
 Carbon loss to oxidation = $(3.273/100) \times (91+3) = 3.07662 \text{kg}$
 The heat of formation of MnO given as :

$$\Delta H_{\text{MnO}_3} = -35205 \text{ cal / mole}$$

One mole of MnO contains 54.99kg of manganese.
 $54.99 \text{kg of Fe} = 35205 \text{ cal} = 147861 \text{ J}$

$$0.83239 \text{kg of Fe} = \frac{0.83239 \times 147861}{54.99} = 2238.19 \text{ J}$$

The heat of formation of SiO_2 expressed as :

$$\Delta H_{\text{SiO}_2}^0 = -88618 \text{ cal / mole}$$

One mole of SiO_2 contains 28.09kg of silicon.
 $28.09 \text{kg of Si} = 88618 \text{ cal} = 372195.6 \text{ J}$

$$2.3012 \text{kg of Si} = \frac{0.83239 \times 372195.6}{28.09} = 11029.26 \text{ J}$$

Ambient temperature, $T_a = 303 \text{K}$

The temperature of molten iron at the center of the cupola, $T_m = 1923 \text{K}$

The inner radius of insulation, $r_1 = 0.23 \text{m}$

The outer radius of insulation, $r_2 = 0.34 \text{m}$

The outer radius of steel shell, $r_3 = 0.35 \text{m}$

Thermal conductivity of alumina (Al_2O_3) refractory lining, $k_1 = 0.000056 \text{W/mK}$

Thermal conductivity of steel shell, $k_2 = 0.24713 \text{W/mK}$

Convective heat transfer coefficient of air, $h_a = 0.025862 \text{W/m}^2\text{K}$

Convective heat transfer coefficient of molten iron, $h_m = 3000 \text{W/m}^2\text{K}$

Cupola height, $L = 5.65 \text{m}$

The density of air, $D_a = 1.2 \text{kg/m}^3$

The volume of hot air blast, $V_r = 450 \text{m}^3$

Specific heat capacity of hot air blast, $C_{pa} = 1005 \text{J/kg K}$

The temperature of hot air blast, $T_{ha} = 973 \text{K}$

Specific heat capacity of iron, $C_{piron} = 1.6 \text{J/kg K}$

Specific heat capacity of coke, $C_{pcoke} = 850 \text{J/kg K}$

Specific heat capacity of limestone, $C_{plux} = 910 \text{J/kg K}$

Exhaust gas temperature, $T_{exh} = 573 \text{K}$

Calorific value of coke, $C_{coke} = 15000000 \text{J/kg}$

Table 1: Cupola critical parameters[8]

Melting capacity(tons)	¾-1	2.25-3	6-6.5
Shell diameter(cm)	69	112	168
Shell diameter with lining(cm)	46	76	112
Shell plate thickness (cm)	0.5	0.7	0.8
Cupola height (cm)	565	750	900

V. COMPUTATIONAL ALGORITHMIC CODING

% COMPUTER SIMULATION OF COMBUSTION AND HEAT LOAD ANALYSIS FOR OPTIMAL USE

% OF CUPOLA FURNACE IN IRON AND STEEL MANUFACTURE

% INITIALIZATION OF PARAMETERS

% T_a --AMBIENT TEMPERATURE (K)

$T_3 = 395.7$;

% T_m --TEMPERATURE OF MOLTEN IRON (K)

$T_m = 1923$;

% r_1 --INNER RADIUS OF INSULATION (m)

$r_1 = 0.23$;

% r_2 --OUTER RADIUS OF INSULATION(m)

$r_2 = 0.305$;

% r_3 --OUTER RADIUS OF THE STEEL SHELL (m)

$r_3 = 0.35$;

% k_1 --THERMAL CONDUCTIVITY OF OF ALUMINA (Al_2O_3) REFRACTORY(W/mK)

% ALUMINA AT 1773k

$k_1 = 0.000056$;

% k_2 --THERMAL CONDUCTIVITY OF STEEL SHELL (W/mK)

$k_2 = 0.24713$;

% h_a --CONVECTIVE HEAT TRANSFER COEFFICIENT OF AIR (W/m²K)

$h_a = 0.0258621$;

% h_m --CONVECTIVE HEAT TRANSFER COEFFICIENT MOLTEN IRON (W/m²K)

$h_m = 3000$;

% FILE TEMP.COM

% SOLVE FOR TEMPERATURES T1, T2 AND T3

$A1 = [(r1 * h_m), 0, (r3 * h_a)]$;

```

A2=[(k1*log(r3/r2)),-(
((k1*log(r3/r2))+(k2*log(r2/r1))), (k2*log(r2/r1))];
A3=[(r1*hm*log(r3/r2)),k2,-k2];
A=[A1;A2;A3];

b=[(r1*hm*Tm+r3*ha*Ta);0;(r1*hm*log(r3/r2)*Tm)
];
Temp=A\b;
disp(Temp)
disp('TEMPERATURE AT THE CURVED
SURFACE OF THE STEEL SHELL, Ta')
fprintf('%20.12f\n',T3)
% CUPOLA ENERGY CONTENT PER UNIT
TIME, Q, IN (Watts)
% L--HEIGHT OF CUPOLA (m)
L=5.65;
Q=((2*pi*L*(Tm-
T3))/((1/(r1*hm))+log(r2/r1)/k1+(log(r3/r2)/k2)+(1/
(r3*ha))))*(24*3600);
disp('HEAT CONTENT OF THE SYSTEM,
Qsystem=')
fprintf('%20.12f\n',Q)
% PERFORMING HEAT BALANCE IN THE
DIFFERENT ZONES OF THE CUPOLA
% HEAT CONTENT OF THE HOT AIR BLAST,
Qhotair (Watts)
% Da--HOT AIR BLAST DENSITY (kg/m3)
Da=1.2;
% Vr--VOLUMETRIC FLOW RATE OF THE
HOT AIR BLAST, Vr (m/s)
Vr=900;
% Cpa--SPECIFIC HEAT CAPACITY OF THE
HOT AIR BLAST (J/kgK)
Cpa=1005;
% Tha--TEMPERATURE OF THE HOT AIR
BLAST (K)
Tha=973;
% Qhot=(0.00001157)*(Da*Vr^Cpa*(Tha-T3);
Qhot=Da*Vr*Cpa*(Tha-T3);
disp('HEAT CONTENT OF THE HOT AIR
BLAST, Qhotair=')
fprintf('%20.12f\n',Qhot)
% Cpiron--SPECIFIC HEAT CAPACITY OF IRON
(J/kgK)
Cpiron=1.65;
% Cpiron--SPECIFIC HEAT CAPACITY OF
COKE (J/kgK)
Ccoke=850;
% Cpiron--SPECIFIC HEAT CAPACITY OF
LIMSTONE (W/kgK)
Cpflux=910;
% HEAT BALANCE IN THE STACK ZONE,
Qstack (Watts)
% EXHAUST GAS TEMPERATURE, Texh (K)
Texh=573;
Qstack=Da*Vr*Cpa*(Texh-T3);
% HEAT BALANCE IN THE PREHEAT ZONE,
Qphz (Watts)
Qphz=((906*Cpiron)+(91*Ccoke)+(3.62*Cpflux))*
(1373-T3);
disp('HEAT CONTENT OF THE PREHEAT
ZONE, Qphz=')
fprintf('%20.12f\n',Qphz)
% HEAT BALANCE IN THE MELTING ZONE,
Qmz (Watts);
Qmz=((906*Cpiron)+(91*Ccoke)+(3.62*Cpflux))*
(1873-T3);
disp('HEAT CONTENT OF THE MELTING
ZONE, Qmz=')
fprintf('%20.12f\n',Qmz)
% HEAT BALANCE IN THE REDUCING ZONE,
Qmz (Watts)
Qrz=((906*Cpiron)+(91*Ccoke)+(3.62*Cpflux))*
(1573-T3);
disp('HEAT CONTENT OF THE REDUCING
ZONE, Qrz=')
fprintf('%20.12f\n',Qrz)
% HEAT BALANCE IN THE COMBUSTION
ZONE, Qmz (Watts)
Qcz=((906*Cpiron)+(91*Ccoke)+(3.62*Cpflux))*
(2123-Ta);
disp('HEAT CONTENT OF THE COMBUSTION
ZONE, Qcz=')
fprintf('%20.12f\n',Qcz)
% HEAT INPUT, Qcal, TO THE SYSTEM DUE
TO CALORIFIC VALUE OF COAL (Watts)
% HEAT EVOLUTION DUE TO OXIDATION OF
CARBON TO CARBON DIOXIDE ( CARBON
LOSS=3.4%, Qcar(Watts)
% Qcar=1.1721;
Qcar=101267.4;
% HEAT EVOLUTION DUE TO OXIDATION OF
IRON TO HAEMATITE (IRON LOSS=3.4%,
% Qfe(J)
Qfe=205650.2;
% HEAT EVOLUTION DUE TO OXIDATION OF
MANGANESE TO MANGANESE OXIDE
% MANGANESE LOSS=15%, Qmn(J)
Qmn=2238.19;
% HEAT EVOLUTION DUE TO OXIDATION OF
SILICON TO SILICON DIOXIDE (SILICON
LOSS=10%, Qsi(J)
Qsi=11029.267;
% HEAT CONTENT OF COKE PER HEAT PER
DAY, Qcoke (J)
% MASS OF COKE, m(KG)
m=94;
% CALORIFIC VALUE OF COKE, Ccoke (J/kg)
Ccoke=15000000;
Qcoke=(m*Ccoke);
disp('HEAT CONTENT OF COKE, Qcoke=')
fprintf('%20.12f\n',Qcoke)
% HEAT ADDITION DUE TO ALL OXIDATION
REACTION, Qoxis (WATTS)

```

```

Qoxi=(Qcar+Qfe+Qmn+Qsi);
disp('HEAT ADDITION DUE TO OXIDATION
REACTION, Qoxi=')
fprintf('%20.12f\n',Qoxi)
% DETERMINATION OF CUPOLA EFFICIENCY,
E(%)
E=(Qphz+Qmz+Qcz)/(Qcoke+Qoxi+Qhot-Q-
Qstack-Qrz);
disp('CUPOLA EFFICIENCY, E=')
fprintf('%20.12f\n',E)
    
```

RESULTS AND DISCUSSIONS

The results of the computational analysis are in Table 2 below:

r ₁ (m)	r ₂ (m)	r ₃ (m)	Thermal Efficiency, E(%)	Shell surface temperature, T ₃ (K)	Refractory lining thickness, t _{ref} (m)	Shell thickness, t _s (m)
0.23		0.35	19.81	385.7	0.115	0.005
0.23		0.35	19.8	386.5	0.11	0.01
0.23		0.35	19.75	387.5	0.105	0.015
0.23		0.35	19.77	388.5	0.1	0.02
0.23		0.35	19.75	389.6	0.05	0.025
0.23		0.35	19.73	390.9	0.09	0.03
0.23		0.35	19.71	392.3	0.085	0.035
0.23		0.35	19.69	293.9	0.08	0.04
0.23		0.35	19.66	395.7	0.075	0.045

The refractory lining and steel shell thickness were varied within reasonable limits. The maximum thermal efficiency of 19.81% was obtained when the refractory lining thickness was 115mm, and the steel shell thickness was 5mm. Improvement in thermal efficiency could obtainable by changing the type of fuel employed in firing the furnace, proper refractory lining selection, among others.

VI. RECOMMENDATION FOR FUTURE RESEARCH

- (i) The computer-simulated algorithmic coding should be modeled with refractories of different insulation properties. This procedure is to determine their effectiveness to conserve heat in the workspace. This stuff is one of the major determinant factors controlling the furnace thermal performance.
- (ii) Different grades of fuels should be applied, and the thermal performance of the cupola measured.

VII. CONCLUSIONS

The computer simulation determined the cupola thermal performance, in reality, was appreciable at 19.81% employing alumina refractory. Literature-based on the works of other researchers, mainly on design, construction, and experimental approach, estimated 30% to 50%.

NOMENCLATURE

- V_{rs} -volumetric of air required per heat (m³)
- T_m—the temperature at the center of the furnace (K)
- Q -heat loss from the surface of the steel shell (J)
- Q_{iron} -thermal load of iron (J)
- Q_{flux} -thermal load of flux (J)
- Q_{coke} -thermal load of coke (J)
- ΔT_{hotair} -the temperature difference of the hot air blast and the surroundings (K)
- ΔT -the temperature difference of Iron, coke and the melt (K)
- T_a—ambient temperature (K)
- T₃—the temperature at the external surface of the steel shell (K)
- T₂—interfacial temperature between the lining and the stell shell K)
- T₁—the temperature at the inner surface of the lining (K)
- R_{th}—thermal resistance (K/W)
- r—radial positions from the center of the furnace (m)
- L—the height of the furnace (m)
- k₂—thermal conductivity of the steel shell K)
- k₁—thermal conductivity of the furnace lining W/mK)
- A_r -the internal and external surface area of the lining and the steel shell (m²)
- h_m—convective heat transfer coefficient of the hot melt (W/mK)
- q̇_r -heat transfer rate per unit mass (Watts)
- Q_{SZ} --heat content per unit time of the flue gases in the stack zone (J)
- Q_{RZ} --heat content per unit time in the reducing zone (J)
- Q_{PHZ} --heat content in the preheat zone (J)
- Q_{MZ} --heat content in the melting zone (J)
- Q_{CZ} --heat content in the combustion or superheat zone (J)
- h_a—convective heat transfer coefficient of the surroundings (W/mK)
- ρ_{air} -the density of air (kg/m³)
- C_{piron}—specific heat capacity of iron (J/kg K)
- C_{pflux}—specific heat capacity of flux (J/kg K)
- C_{pcoke}—specific heat capacity of coke (J/kg K)
- ΔT_{Overall} -the potential thermal difference (K)

H1—stack zone height (m)
H2—preheat zone height (m)
H3—melting zone height (m)
H4—reducing zone height (m)
H5—combustion zone height (m)
H6—well zone height (m)
 ΔT_{H1} -the temperature difference of the hot effluent gases in the stack zone (K)
 ΔT_{H2} -the temperature difference in the preheat zone (K)
 ΔT_{H3} -the temperature difference in the melting zone (K)
 ΔT_{H4} -the temperature difference in the reducing zone (K)
 ΔT_{H5} -the temperature difference in the combustion zone (K)
 ΔT_{H6} -the temperature difference in the well region (K)

REFERENCES

- [1] Izumi Oishi, Hisato Nimomiya, Kenje Kawashima-Talkabutsu refractories 1980-No 8-P8. - P35-38.
- [2] Abbakumov V. G., Tsibin I. P. , Nivikov V. L. Dsigning efficient Industrial Unit // Lining refractories- 1987—52, No 5. P822-827.
- [3] Golle Daniel Resource-friendly refractories technologies for the cupola furnace // Get and Technol. Int. -2011.-27, No 3. -P14-16.
- [4] Energieeffiziente Auskeldung von Bvennofe n// Stal.und Eisen-2013—133, No 8.-P 46.
- [5] Intelligent Control of Cupola Melting E. D., Larsen. Et.All. Lockheed Martin Idaho Technologies Company, June 1997.
- [7] British Cast Iron Research Association : Cupola design, Operation and Control. (1st edition) BCIRA 1979.
- [8] Fine A. H. , Geiger H., Handbook on Material and Energy balance calculation in Metallurgical Process, 1980.
- [9] O.P. KHANNA, “A Text Book of Material Science and Metallurgy “, Dhanpat Rai Publication (P) Ltd, New Delhi-110002, 1999. ISBN Ph : 2327 4073 2324 6573
- [10] Tobinson A. Briggs and Shadrack Mathew Uzoma “Heat Load Analysis For Optimal Use Of Cupula Furnace In Iron Castings And Steel Manufacturing” European Journal of Mechanical Engineering Research, Vol.6, No.1, pp.32-43, April 2019, Print ISSN: ISSN 2055-6551(Print), Online ISSN: ISSN 2055-656X(Online)