

Determination of Optimal Torque in Thread Rolling Operation

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Abstract: Manufacturing of threads, splines and gears will be conventionally done using metal cutting (chip flowing process). In the chip flow process, continuity and the strength of component gets decreased. Alternatively the above general components can also be manufactured by using metal forming in which the metal grain boundaries continuity remains and the components can withstand to higher loads. At present for cold forming for different work material and roll combinations, an empirical (approximate) solution is used for determining the torque requirements of motor. An attempt is being made to study the forming forces in thro feed of the component at roll and work intersection and to determine the optical torque requirement using ANSYS software. To generalize the thread rolling process, software code is developed which can be used for different Work –Tool combinations to estimate the torque requirements.

Keywords: Analysis, Cold forming, Discretization, Grain boundaries, Optimal Torque, Thread rolling.

I. INTRODUCTION

Thread Rolling is a process of making external threads. Threads are made through a die which is a hardened tool with the thread profile. The workpiece fixed with a rotor. The rotor turns around the metal piece and die creates a force, and the force results threads on the metal piece. As the force increases gradually, the accurate thread profile is transferred to the workpiece. This process produces screws with greater strength. During the process, the surface layer of the raw material is put into compressive stress.

Read forming and thread rolling are processes for forming screw threads, with the former referring to creating internal threads and the latter external threads. In both of these processes threads are formed into a blank by pressing a shaped die against the blank, in a process similar to knurling. These processes are used for large production runs because typical production rates are around one piece per second. Forming and rolling produce no swarf and less material is required because the blank size starts smaller than a blank required for cutting threads; there is typically a 15 to 20% material savings in the

blank, by weight. A rolled thread can often be easily recognized because the thread has a larger diameter than the blank rod from which it has been made; however, necks and undercuts can be cut or rolled onto blanks with threads that are not rolled. Also, the end of the screw usually looks a bit different from the end of a cut-thread screw



Fig 1: Rolling

II. DIMENSIONS AND STRUCTURE OF MATERIALS

High Speed Steel (Rollers)
Composition – 18% tungsten, 4% chromium, 1% vanadium

Mild steel (Work)
Composition – 0.35-0.45% carbon, 0.05-0.35% silicon, sulphur and phosphorus less than 0.06%.

- Diameter of the roller = 170mm
- Diameter of the job = 50mm
- Length of the roller and job = 130mm
- Thread depth – 3.25mm
- Pitch – 5mm

Thread profile – v-thread

III. MATHEMATICAL CALCULATION FOR TORQUE

Motor power = 3.7kW = 5hp

Speed = 1500rpm

Power (p) = Torque (T) * Angular velocity (ω)

Torque, T = $3.7 \times 1000 \times 60 / (2 \times \pi \times 1500) = 23.554 \text{ N-m}$

Maximum speed of the roll shaft = 84rpm

Power(p) = Torque (T) * Angular velocity(ω)
 Torque, T = $3.7*60*1000/(2*\pi*84) = 420.623$ N-m
 Torque = Force * radius of the roller
 Radius of the roller = 0.085m
 Length of the roller = 0.130m
 Force = $420.623/0.085 = 38.065$ N
 Force per unit length = Force/0.130 = $38.065/0.130 = 4.94845$ N-m

IV. CONTACT STRESSES APPROACH FOR THREAD ROLLING TO FIND OUT THE TORQUE

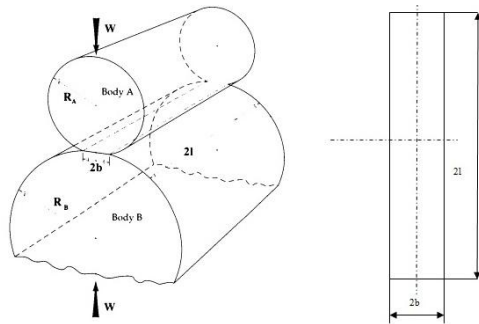


Fig 2: 2d Diagram of Rolling

where,
 b is the half width of the contact rectangle [m]
 l is the half length of the contact rectangle [m]
 R1 is the reduced radius of curvature for two parallel cylinders in contact [m]. For the cylinders $R_{ax} = R_A$, $R_{bx} = R_B$, where R_A and R_B are the radii of the cylinders A and B, respectively.
 $1/R_x = 1/R_{ax} + 1/R_{bx} = 51.7645$ 1/m
 R_{ax} = Radius of the roller
 R_{bx} = Radius of the job
 $1/R_y = \infty$
 Reduced radius of curvature:
 $1/R^* = 1/R_x = 51.7645$ 1/m
 $R^* = 0.019318$ m
 Reduced young's modulus
 $1/E^* = 1/2[(1-\nu_A^2)/E_A + (1-\nu_B^2)/E_B] = 5.6228*10^{-8}$ m²/N
 Where E_A = Youngs modulus of the Roller = $210*10^9$ N/m²
 E_B = Youngs modulus of the job = $200*10^9$ N/m²
 Contact area dimensions
 $b = 4WR^*/\pi E^* = 0.027$ m
 Maximum and average contact pressure
 $P_{max} = W/\pi b l = 4448176.615$ N/m² = 4.4481 MPa
 $P_{average} = W/4bl = 3493589$ N/m² = 3.4936 MPa
 Maximum deflection
 $\delta = 0.319[W/E^*I][2/3 + \ln(4R_A R_B/b^2)] = 0.01125$ m
 Maximum shear stress
 $\tau_{max} = 0.304 P_{max}$
 $\tau_{max} = 1.216$ MPa
 Depth at which maximum shear stress occurs
 $Z = 0.786b = 0.021222$ m

$T/J = \tau / (\text{radius of the roller})$
 $J = \pi/32 (\text{diameter of the roller})^4 = 8.19965*10^{-5}$ m⁴
 $T = 1173.03$ N-m

V. 'C' PROGRAM FOR CONTACT STRESSES

```
#include<stdio.h>
#include<conio.h>
#include<math.h>
void main ()
{
    float
    R,r,rx,ea,eb,e1,b,l,w,a,deflection,pavg,pmax, shear,J,z
    ;
    label:read;
    printf("\nENTER POISONS RATIO OF
    THE ROLLER");
    scanf("%f",&va);
    printf("\nENTER POISONS RATIO OF
    THE JOB");
    scanf("%f",&vb);
    if(va==0.5||vb==0.5)
    {
        printf("\nERROR!!!POISONS
        RATIO YOU ENTERED IS EQUAL TO
        0.5");
        goto read;
    }
    else
    {
        printf("\nENTER THE ROLLER
        RADIUS IN METRES");
        scanf("%f",&R);
        printf("\nENTER THE JOB
        RADIUS IN METRES");
        scanf("%f",&r);
        rx=R*r/(r+R);
        printf("\nENTER THE LENGTH
        OF THE ROLLER");
        scanf("%f",&l);
        printf("\nENTER THE YOUNGS
        MODULUS OF THE ROLLER");
        scanf("%f",&ea);
        printf("\nENTER THE YOUNGS
        MODULUS OF THE JOB");
        scanf("%f",&eb);
        printf("\nENTER THE LOAD
        APPLIED");
        e1=ea*eb/((eb(1-va*va))-(ea(1-
        vb*vb)))
        a=4wra/(3.141*1*e1);
        b=sqrt(a);
        pmax=w/(3.141*b*l);
        pavg=w/(4*b*l);
        shear=0.304*pmax;
        z=0.786*b
        J=3.141*2*R*R*R*R;
        T=J*shear/R;
        printf("\n Half width = %f m \n Maximum pressure =
        %f N-m^2 \n Average pressure = %f N-m^2 \n
```

Maximum shear = $\frac{1}{2} \sqrt{(\sigma_x - \sigma_y)^2 + \tau_{xy}^2}$ \n Maximum shear occurs at the depth of $\frac{1}{2} \sqrt{(\sigma_x - \sigma_y)^2 + \tau_{xy}^2}$ \n Required torque to produce maximum shear stress = $\frac{1}{2} \sqrt{(\sigma_x - \sigma_y)^2 + \tau_{xy}^2} \cdot b \cdot p_{max} \cdot p_{avg} \cdot \text{shear} \cdot z \cdot T$;

}

VI. FINITE ELEMENT METHOD

Element considered: **CST** (Constant Strain Triangle)

Table 1
Element Connectivity

Element	1	2	3
1	1	2	4
2	2	3	4

Element 1 in the following fig 3 represents job element
Element 2 in the following fig 3 represents the roller element

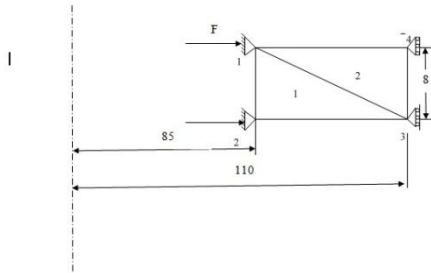


Fig 3: Free body diagram.

Table 2
Nodal points

Node	r	z
1	85	8
2	85	0
3	110	0
4	110	8

The units of millimeters for length, N for force, MgaPascals for stress and E. These units are consistent

Element 1

D_1 =Elastic material matrix for roller
 B_1 =Strain displacement matrix for roller
 K_1 =Stiffness matrix for roller

$$D_1 = \frac{E}{(1-\nu)(1+\nu)(1-2\nu)} \begin{pmatrix} 1 & \nu & 0 & \nu \\ \nu & 1 & 0 & \nu \\ 0 & 0 & (1-2\nu)/2 & 0 \\ \nu & \nu & 0 & 1 \end{pmatrix}$$

E =modulus of elasticity of the roller
Roller material = High speed steel
 E for Roller=210GPA
 ν =poisons ratio=0.3

$$D_1 = \begin{pmatrix} 269000 & 115000 & 0 & 115000 \\ 115000 & 269000 & 0 & 115000 \\ 0 & 0 & 77000 & 0 \\ 115000 & 115000 & 0 & 269000 \end{pmatrix}$$

$$B_1 = \begin{pmatrix} z_{31}/\det J & 0 & z_{31}/\det J & 0 & z_{12}/\det J & 0 \\ 0 & r_{32}/\det J & 0 & r_{13}/\det J & 0 & r_{31}/\det J \\ r_{32}/\det J & z_{31}/\det J & r_{13}/\det J & z_{31}/\det J & r_{31}/\det J & z_{12}/\det J \\ N_1/r & 0 & N_2/r & 0 & N_3/r & 0 \end{pmatrix}$$

$$B_1 = \begin{pmatrix} -0.04 & 0 & 0 & 0 & 0.04 & 0 \\ 0 & 0.1250 & 0 & -0.1250 & 0 & 0 \\ 0.125 & -0.04 & -0.125 & 0 & 0 & 0.04 \\ 0.0035 & 0 & 0.0035 & 0 & 0.0035 & 0 \end{pmatrix}$$

$$D_1 * B_1 = \begin{pmatrix} -10357.5 & 14375 & 402.5 & -14375 & 11162.5 & 0 \\ -4197.5 & 33625 & 402.5 & -33625 & 5002.5 & 0 \\ 9625 & -3080 & -9625 & 0 & 0 & 3080 \\ -3658.5 & 14375 & 941.5 & -14375 & 5541.5 & 0 \end{pmatrix}$$

$$B^T = \begin{pmatrix} -0.04 & 0 & 0.1250 & 0.0035 \\ 0 & 0.1250 & -0.04 & 0 \\ 0 & 0 & -0.1250 & 0.0035 \\ 0 & -0.1250 & 0 & 0 \\ 0.04 & 0 & 0 & 0.0035 \\ 0 & 0 & 0.04 & 0 \end{pmatrix}$$

Now the stiffness matrix of element 1 can be found out as follows
 $K^e = 2\pi \bar{r} A_c \bar{B}^T D \bar{B}$
 $A_c = 0.5 |\det J|$
 \bar{r} =centroid=93.333

$$|\det J| = r_{13}z_{23} - r_{23}z_{13}$$

$$|\det J| = (85-110)(0-0) - (85-110)(8-0)$$

$$= -(85-110)(8)$$

$$= 200$$

$$|\det J| = 200$$

$$A_e = 0.5 * 200$$

$$= 100$$

$$K_1 = 53407.075 \begin{pmatrix} 1604.6203 & -909.6875 & 1215.9298 & 524.6875 & -427.1048 & 385 \\ 909.6875 & 4326.3250 & 435.3125 & -4203.1250 & 625.3125 & -123.2 \\ -1215.9298 & 435.3125 & 1206.4203 & -50.3125 & 19.3953 & 385 \\ 524.6875 & -4203.125 & -50.3125 & 4203.1250 & -625.3125 & 0 \\ -427.1048 & 625.3125 & 19.3953 & -625.3125 & 465.8953 & 0 \\ 385 & -123.2 & -385 & 0 & 0 & 123.2 \end{pmatrix}$$

Element 2:

D_2 =Elastic material matrix for the job
 B_2 =Strain displacement matrix for the job
 K_2 =Stiffness matrix
 E =Modulus of elasticity of the job(mild steel)=200GPA

$$D_2 = (E(1-\nu)/((1+\nu)(1-2\nu))) \begin{pmatrix} 1 & \nu/(1-\nu) & 0 & \nu/(1-\nu) \\ \nu/(1-\nu) & 1 & 0 & \nu/(1-\nu) \\ 0 & 0 & (1-2\nu)/2(1-\nu) & 0 \\ \nu/(1-\nu) & \nu/(1-\nu) & 0 & 1 \end{pmatrix}$$

ν =poisons ratio=0.3

$$D_2 = \begin{pmatrix} 282000 & 121000 & 0 & 121000 \\ 121000 & 282000 & 0 & 121000 \\ 0 & 0 & 80560 & 0 \\ 121000 & 121000 & 0 & 282000 \end{pmatrix}$$

$$B_2 = \begin{pmatrix} -0.04 & 0 & 0.04 & 0 & 0 & 0 \\ 0 & 0 & 0 & -0.125 & 0 & 0.1250 \\ 0 & -0.04 & -0.1250 & 0.04 & 0.1250 & 0 \\ 0.0032 & 0 & 0.0032 & 0 & 0.0032 & 0 \end{pmatrix}$$

$$D_2 * B_2 = \begin{pmatrix} -10892.8 & 0 & 11667.2 & -15125 & 387.2 & 15125 \\ -4452.8 & 0 & 5227.2 & -35250 & 387.2 & 35250 \\ 0 & -3222.4 & -10070 & 3222.4 & 10070 & 0 \\ -3937.6 & 0 & 5742.4 & -15125 & 902.4 & 15125 \end{pmatrix}$$

$$B^T = \begin{pmatrix} -0.04 & 0 & 0 & 0.0032 \\ 0 & 0 & -0.04 & 0 \\ 0.04 & 0 & -0.125 & 0.0032 \\ 0 & -0.1250 & 0.04 & 0 \\ 0 & 0 & 0.1250 & 0.0032 \\ 0 & 0.1250 & 0 & 0 \end{pmatrix}$$

$$K^e = 2\pi \bar{r} A_e \bar{B}^T D \bar{B}$$

$$A_e = 0.5 |\det J|$$

$$\bar{r} = \text{centroid} = 101.6667$$

$$K_2 = 15707.96 \begin{pmatrix} 423.112 & 0 & -448.312 & 556.6 & -12.6 & -556.6 \\ 0 & 128.896 & 402.8 & -128.896 & -402.8 & 0 \\ -448.312 & 402.8 & 1743.814 & -1056.2 & -1240.374 & 653.4 \\ 556.6 & -128.896 & -1056.2 & 4535.146 & 354.4 & -4406.25 \\ -12.6 & -402.8 & -1240.374 & 354.4 & 1261.638 & 48.4 \\ -556.6 & 0 & 653.4 & -4406.25 & 48.4 & 4406.25 \end{pmatrix}$$

Using the elimination approach, on assembling the matrices with reference to the degrees of freedom 1 & 3

$$K = \begin{pmatrix} 85698000 & -64939000 \\ -64939000 & 71077000 \end{pmatrix}$$

The force supplied by the Hydraulic power pack is a traction force.

So the Roller exhibits traction force on the job.

$$F_1 = F_3 = 2 * \pi * r_1 * l_e * p_i / 2$$

Where r_1 =Radius of the roller=85mm

l_e =sample length=8mm

$$P_i = 3.4936 \text{MPa}$$

Hence the force vector is obtained as follows

$$F = \begin{pmatrix} 7463.9592 \\ 7463.9592 \end{pmatrix}$$

$$K * Q = F$$

$$Q = \begin{pmatrix} 0.0005 \\ 0.0006 \end{pmatrix}$$

$$\sigma_1 = D_1 B_1 Q_3$$

$$Q_1^T = [0.0005 \ 0 \ 0.0006 \ 0 \ 0 \ 0 \ 0]^T$$

$$Q_2^T = [0.0006 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0]^T$$

$$D_1 \cdot B_1 = \begin{pmatrix} -10357.5 & 14375 & 402.5 & -14375 & 11162.5 & 0 \\ -4197.5 & 33625 & 402.5 & -33625 & 5002.5 & 0 \\ 9625 & -3080 & -9625 & 0 & 0 & 3080 \\ -3658.5 & 14375 & 941.5 & -14375 & 5541.5 & 0 \end{pmatrix}$$

$$Q_1 = \begin{pmatrix} 0.0005 \\ 0 \\ 0.0006 \\ 0 \\ 0 \\ 0 \end{pmatrix}$$

$$\sigma_1 = D_1 B_1 Q_1 = \begin{pmatrix} -4.9373 \\ -1.8573 \\ -0.9625 \\ -1.2644 \end{pmatrix}$$

Where σ_1 = Stress matrix for the roller

$$D_2 \cdot B_2 = \begin{pmatrix} -10892.8 & 0 & 11667.2 & -15125 & 387.2 & 15125 \\ 4452.8 & 0 & 5227 & -35250 & 387.2 & 35250 \\ 0 & -3222.4 & -10070 & 3222.4 & 10070 & 0 \\ -3937.6 & 0 & 5742.4 & -15125 & 902.4 & 15125 \end{pmatrix}$$

$$Q_2 = \begin{pmatrix} 0.0006 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \end{pmatrix}$$

$$\sigma_2 = D_2 B_2 Q_2 = \begin{pmatrix} -6.5357 \\ -2.6717 \\ 0 \\ -2.3626 \end{pmatrix}$$

Where σ_2 = stress matrix for the job

From the σ_1 matrix, maximum shear stress
 $\tau = 0.9625 \text{ MPa}$

Now the torque can be found out from the torsion equation $T/J = \tau/r$

Where,

T = torque

J = Polar moment of inertia

τ = Shear stress

r = Radius of the roller = 85mm

$J = \pi/32$ (diameter of the roller)⁴

$T = (\pi/32 (170)^4) * 0.9625/85$

= 928490.3457 N-mm = 928.490 N-m

Hence torque due to shear stress = 928.490 N-m

VII. ANSYS-RESULTS

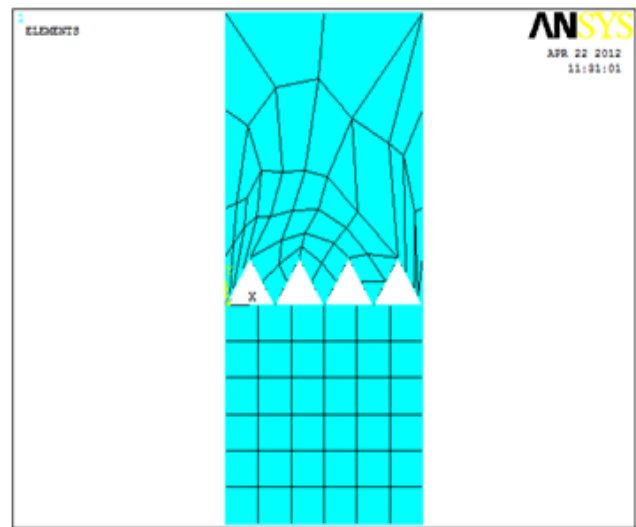


Fig 4: Stress diagram 1

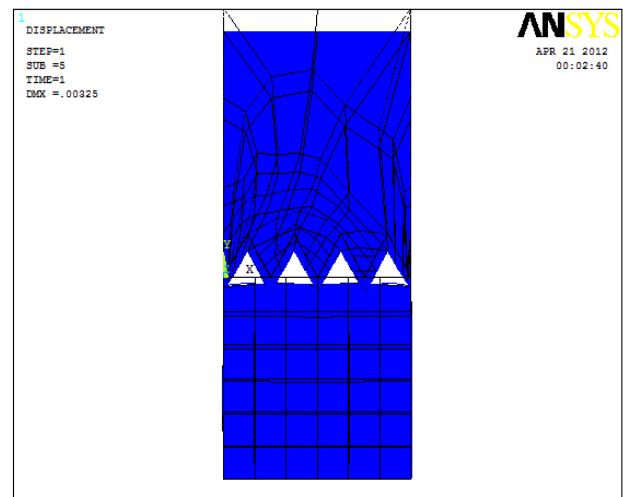


Fig 5: Stress diagram 2

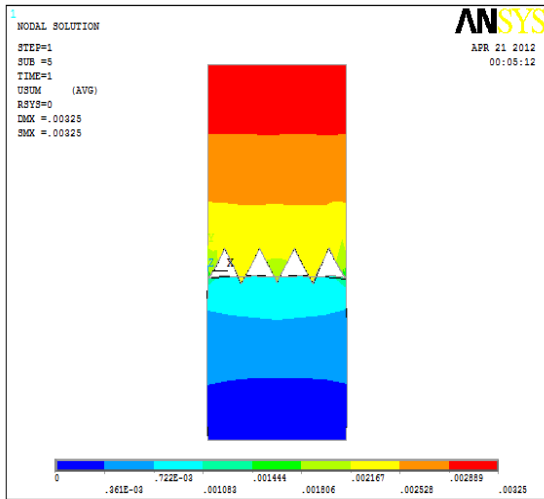


Fig 6: Stress diagram 3

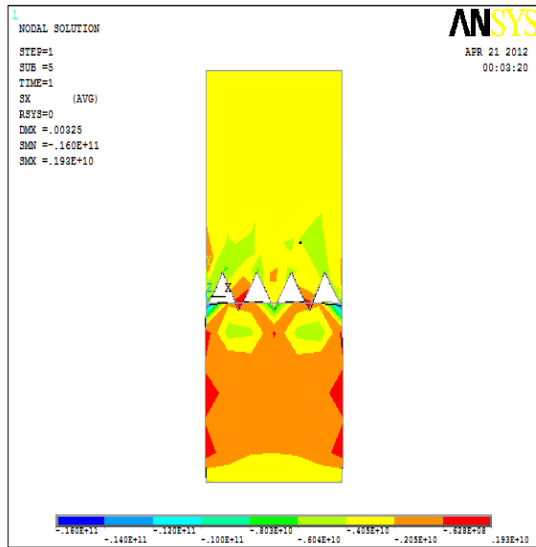


Fig 7: Stress diagram 4

VIII. CONCLUSION

The torque obtained by contact stresses approach and FEM are almost in the equal range In ANSYS, the stress intensity obtained is maximum at cutting edges and the results obtained are within the allowable stresses. The strain hardening affect is not taken into consideration in any of the approaches.

Table 2:
Comparison Table

S.NO	METHOD	TORQUE (ONE ROLLER) N-m
1	Contact stresses	1173.03
2	FEM	928.490

IX. FUTURE SCOPE

This can further be extended by taking strain hardening affect into account and also dynamic analysis can be performed to obtain optimal torque.

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Conflict of Interest: Nil

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