

Comparative Study of Data Transmission Techniques of Different Block Codes over AWGN Channel using Simulink

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Abstract-Channel Coding is the process of adding redundant data bits to a digital data stream which facilitates in reduction in the BER caused by noise in the transmission channel. This paper presents a study of various block code namely Hamming code, Bose-Chaudhuri-Hocquenghem (BCH) and Low density Parity Check code (LDPC). In order to analyse a communication link with AWGN Channel, and different modulations, Matlab is used for simulation. The simulation helps in better estimating the performance of such system because they are very easy to implement as compared to analytical methods which prove to be too complicated. LDPC have gained popularity in recent year and moreover it claims the performance near Shannon limit. In this paper LDPC performs better as compared to other block codes. Moreover BCH is having better performance in comparison to Hamming code because it is an extension of hamming code and having better result with small value of E_b/N_0 whereas Hamming code is having better performance with large value of E_b/N_0 whereas Without coding is having the worst performance in comparison to all the method. These results are plotted using BERTOOL in communication system tool. The comparison is based on the results to understand better performance of these codes.

Keywords-Channel Coding, Hamming Codes, Simulink, BCH, LDPC.

I. INTRODUCTION TO CODING THEORY

Coding theory originated with the advent of computers. Early computers were huge mechanical monsters whose reliability was low as compared to the computers of today. As they were based on banks of mechanical relays, if a single relay failed to close the entire calculation was in error. The engineers of the day devised ways to detect faulty relays so that they could be replaced. Setting to work on this problem Hamming devised a way of encoding information so that if an error was detected it could also be corrected. Based in part on this work, Claude Shannon developed the

theoretical framework for the science of coding theory [1].

The following figure provides a rough idea of general information about transmission process of a message.

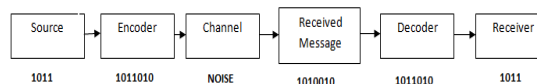


Fig1: Example of how a data move from source to receiver

The output of an information source is a continuous sequence of binary symbols over Generator function called an information sequence. The binary symbols in an information sequence are commonly called information bits, where a bit stands for a binary digit. In block coding, an information sequence is segmented into message blocks of fixed length; each message block consists of k information bits.[8] There are 2^k distinct messages. At the channel encoder, each input message $u = (u_0, u_1, \dots, u_{k-1})$ of k information bits is encoded into longer binary sequence $v = (v_0, v_1, \dots, v_{n-1})$ of n binary digits with $n > k$, according to certain encoding rules. This longer binary sequence v is called the codeword are called code bits. Since there are 2^k distinct message, there are 2^k codewords, one for each distinct message. This set of 2^k codewords is said to form an (n, k) block code. For a block code to be useful, the 2^k codewords for the 2^k distinct message must be distinct. The $n-k$ bits added to each input message by the channel encoder are called redundant bits[4]. These redundant bits carry no new information and their main function is to provide the code with capability of detecting and correcting transmission errors caused by the channel noise or interferences. How to form these redundant bits such that an (n, k) block has good error correction capability is a major concern in designing the channel encoder. The ratio $R = k/n$ is called the code rate, which is

interpreted as the average number of information bits carried by each code bit.

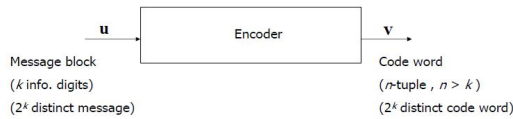


Fig2:Structure of Block Code

For a block code of length n with 2^k codewords, unless it has certain special structural properties, the encoding and decoding apparatus would be prohibitively complex for large k since the encoder has to store 2^k codewords of length n in a dictionary and the decoder has to perform a table (with 2^k entries) lookup to determine that transmitted codeword. The desirable structure for a block code is linearity as shown in figure 2. A binary block code of length n with 2^k codewords is called an (n, k) linear block code if and only if its 2^k codewords form a k -dimensional subspace of the vector space V of all the n -tuples over Generator Function [11].

II. DIFFERENT BLOCK CODING MODELS

There are two structurally different types of codes, block and convolution codes both types of codes have been widely used for error control in communication and storage systems. Block codes can be divided into two categories linear and nonlinear block codes. Nonlinear block codes are never used in practical applications and not much investigated. In block coding, an information sequence is segmented into message blocks of fixed length; each message block consists of k information bits. There are 2^k distinct messages. [3]

A. Without Code Model:

In without coding model basically no coding has been used. It is a simple model containing different modulations and demodulations like BPSK, QPSK, 8PSK and 16PSK and AWGN channel model as shown in figure 3.

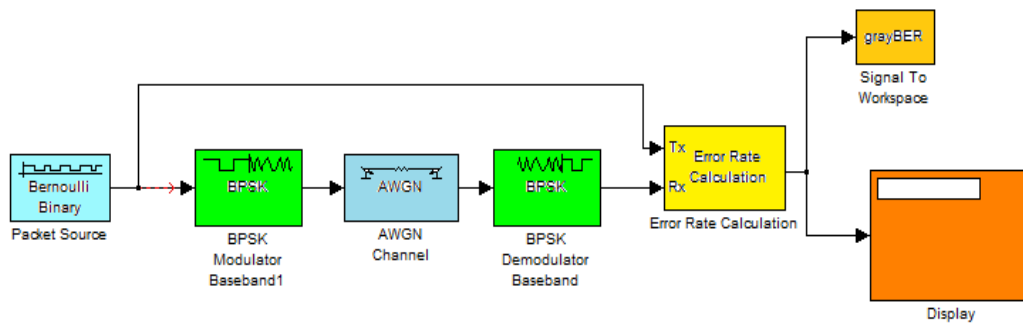


Fig 3: Without Code Model

B. Hamming Code:

In the late 1940's Claude Shannon was developing information theory and coding as a mathematical model for communication. At the same time, Richard Hamming, a colleague of Shannon's at Bell Laboratories, found a need for error correction in his work on computers. Parity checking was already being used to detect errors in the calculations of the relay-based computers of the day, and Hamming realized that a more sophisticated pattern of parity checking allowed the correction of single errors along with the detection of double errors. The codes that Hamming devised, the single-error-correcting binary Hamming codes and their single-error-correcting, double-error-

detecting extended versions marked the beginning of coding theory. These codes and their variations have been widely used for error control in digital communication and data storage systems [7]. Hamming Code model is shown in figure 4.

For any positive integer $m \geq 3$, there exists a Hamming code with the following parameters: [4]

- Code length: $n = 2^m - 1$
- Number of information symbols: $k = 2^m - m - 1$
- Number of parity-check symbols: $n - k = m$
- Error-correcting capability: $t = 1$ ($d_{\min} = 3$).

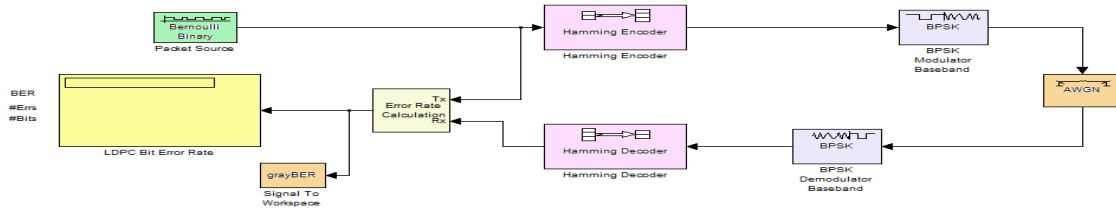


Fig 4: Hamming Code Mode

1)PARAMETER FOR COMMUNICATION LINK WITH HAMMING CODING:

(a) BERNOULLI BINARY

Probability of a zero	Initial seed	Sample time	Samples per frame	Output data type
0.5	61	3.1662e-02	1013	Double

(b) HAMMING ENCODER

Codeword length	Message length K, or M-degree primitive polynomial
1023	gfprimfd(10,'min')

(c) BPSK MODULATION

Phase Offset	Data Type
0	Double

(d) BPSK DEMODULATION

Phase offset (rad)	Decision Type	Output	Derotate Factor
0	Hard Decision	Inherite via Inherite	Same word length

(i) AWGN CHANNEL

I/P Processing	Initial Seed	Mode	Eb/No (dB)	No. of bits per symbol	I/P Signal Power(watts)	Symbol Period
Columns channel	61	SNR (Eb/No)	EbNo	1	1	1

C. BCH Code:

BCH codes are a generalization of Hamming codes, and they can be designed to correct any error pattern of size t or less [1, 2, 4]. In this sense the generalization of the Hamming codes extends the design of codes for $t = 1$ (Hamming codes) to codes for any desired higher value of t (BCH codes). The model is shown in figure5. The design method is based on taking an LCM of appropriate minimal polynomials, as described in the previous section

(e) HAMMING DECODER

Codeword length N	Message length K, or M-degree primitive polynomial
1023	gfprimfd(10,'min')

(f) ERROR RATE CALCULATION

Receive Delay	Computation Delay	Computation Mode	O/P Data	Target no. of Error	Max no. Of Symbol
0	0	Entire frame	Port	100	1e8

(g) SIGNAL TO WORKSPACE

Variable Name	Limit Data point	Decimation	Same Format
Gray BER	1	1	Array

(h) DISPLAY

Format	Decimation
Long	1

for a particular example. For any positive integer $m \geq 3$ and $t < 2m-1$, there exists a binary BCH code $C_{BCH}(n, k)$ with the following properties:[5]
 Code length $n = 2^m - 1$
 Number of parity bits $n - k \leq mt$
 Minimum Hamming distance $d_{min} \geq 2t + 1$
 Error-correction capability t errors in a code vector. These codes are able to correct any error pattern of size t or less, in a code vector of length $n, n = 2^m - 1$.

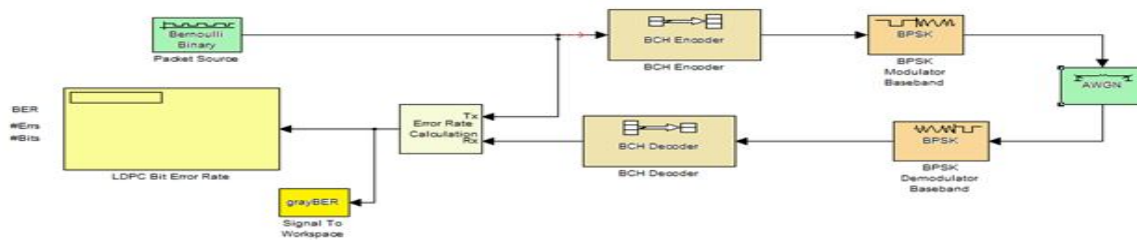


Fig 5: BCH Code Model

1) PARAMETER FOR COMMUNICATION LINK WITH BCH CODING:

(a) BERNOULLI BINARY

Probability of a zero	Initial seed	Sample time	Samples per frame	Output data type
0.5	435345	6.2500e-005	16	Double

(b) BCH ENCODER

Codeword length N	Message length K
31	16

(c) BPSK MODULATION

Phase Offset	Data Type
0	Double

(d) BPSK DEMODULATION

Phase offset (rad)	Decision Type	Output	Derotate Factor
0	Hard Decision	Inherit via Inherit	Same word length

(e) BCH DECODER

Codeword length N	Message length Kdegree
31	16

(f) ERROR RATE CALCULATION

Receive Delay	Computation Delay	Computation Mode	O/P Data	Target no. of Error	Max no. Of Symbol
0	0	Entire frame	Port	100	1e8

(g) SIGNAL TO WORKSPACE

Variable Name	Limit Data point	Decimation	Same Format
Gray BER	1	1	Array

(h) DISPLAY

Format	Decimation
Long	1

(i) AWGN CHANNEL

I/P Processing	Initial Seed	Mode	Eb/No (dB)	No. of bits per symbol	I/P Signal Power(watts)	Symbol Period
Columns channel	123456	SNR (Eb/No)	7	1	1	6.2500e-05

D. LDPC:

Low-density parity-check codes are a class of linear block codes which provide near capacity performance on a large collection of data transmission and storage channels while simultaneously admitting implementable decoder. It is forward error-correction codes, first proposed in the 1962 PhD thesis of Gallager at MIT. At the time, their incredible potential remained

undiscovered due to the computational demands of simulation in an era when vacuum tubes were only just being replaced by the first transistors. They remained largely neglected for over 35 years. One notable exception is the important work of Tanner in 1981 in which Tanner generalized LDPC codes and introduced a graphical representation of LDPC codes, now called Tanner graphs. The name comes from the characteristic of their parity-check matrix which contains only a few 1's in comparison to the

amount of 0's. It's also a bit different from general parity check matrix[14]. The order of matrix in

LDPC is of order n and not n^2 [6].The model is shown in figure 6.

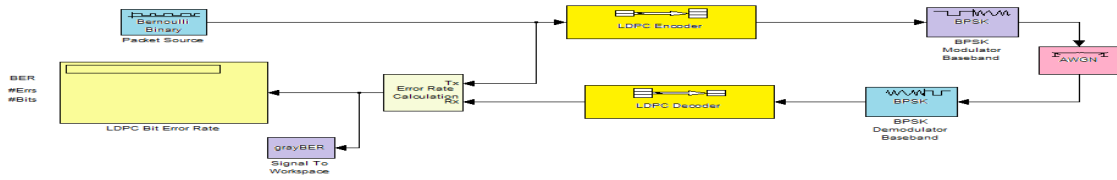


Fig 6: LDPC Code Model

1)PARAMETER FOR COMMUNICATION

LINK WITH LDPC CODING:

(a) BERNOULLI BINARY

Probability of a zero	Initial seed	Sample time	Samples per frame	Output data type
0.5	435345	6.2500e-005	16	Double

(b) LDPC ENCODER

Codeword length N	Message length K
32400	64800

(c) BPSK MODULATION

Phase Offset	Data Type
0	Double

(d) BPSK DEMODULATION

Phase offset (rad)	Decision Type	Output	Derotate Factor
0	Hard Decision	Inherit via Inherit	Same word length

(h) DISPLAY

Format	Decimation
Long	1

(e) LDPC DECODER

Parity check matrix (sparse binary (N-K)-by-N matrix)	O/P Formats	Decision Type	O/P Data Type	No of Iterations
64800	Information point	Hard Decision	Double	50

(f) ERROR RATE CALCULATION

Receive Delay	Computation Delay	Computation Mode	O/P Data	Target no. of Error	Max. No. Of Symbol
0	0	Entire frame	Port	100	1e8

(g) SIGNAL TO WORKSPACE

Variable Name	Limit Data point	Decimation	Same Format
Gray BER	1	1	Array

(i) AWGN CHANNEL

I/P Processing	Initial Seed	Mode	Eb/No (dB)	No. of bits per symbol	I/P Signal Power(watts)	Symbol Period
Columns channel	61	SNR (Eb/No)	10	1	1	1

III. SIMULATION RESULT

In this paper simulation models with Matlab have been designed using various block codes and different modulations and demodulations such bpsk, qpsk, 8psk and 16psk. The BER performance

for each PSK-based transmission scheme under various conditions is studied and identified which modulation scheme gives best BER performance.

A. WITHOUT CODE:

The performance analysis of communication link in various modulation techniques but in without channel coding. It has been observed that at $E_b/N_0 = 4\text{db}$, as shown in figure7, the BPSK modulation signal has 0.4168 BER, QPSK modulation has 0.4178 BER, 8-PSK modulation signal has 0.4266 BER and 16-PSK modulation signal has 0.4325 BER. So it can be concluded that performance of BPSK is best

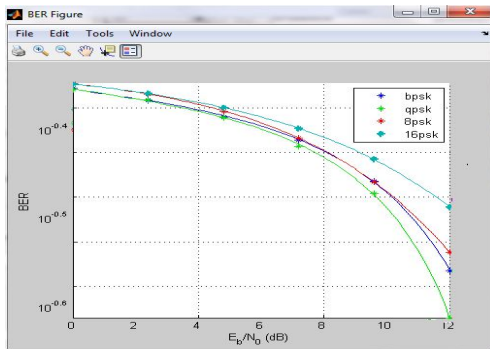


Fig 7:BER for Without-Coding Model

B. HAMMING CODE:

The performance analysis of (1023,10) Hamming code for various modulation technique are shown in figure 8. The BER values for $E_b/N_0 = 4\text{db}$ are 0.3388 BER, 0.3589 BER, 0.3802 BER and 0.4169 BER for BPSK, QPSK, 8-PSK and 16-PSK.

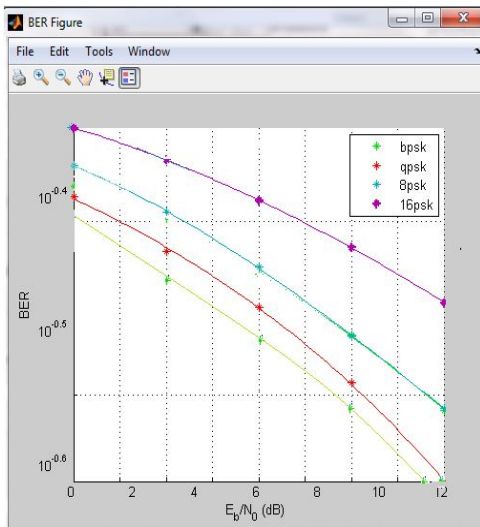


Fig 8:BER for Hamming Code

C. BCH CODE:

BCH codes constitute a powerful class of codes that provides a large selection of block length, code rate and error-correction capability. BCH code used for simulation has $(n,k) = (31,16)$ with code rate is .51. Performance analysis of BCH codes with binary phase shift keying modulation and using a AWGN channel. The result is 0.3090 BER.

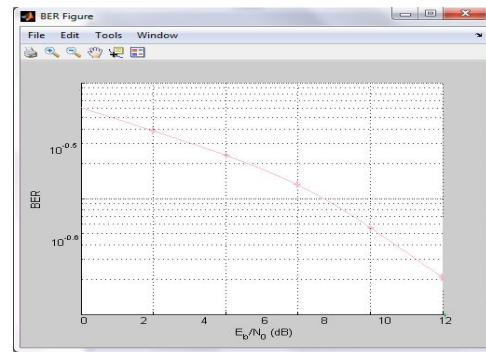


Fig 9:BER for BCH coding Model

D. LDPC CODING:

In case of low Density Parity Check code the code rate used is 1/2 and the message length and code length used is 32400 and 64800 respectively. The BER values for $E_b/N_0 = 4\text{db}$ are 0.2559 BER, 0.2818 BER, 0.2818 BER and 0.3062 BER for BPSK, QPSK, 8-PSK and 16-PSK.

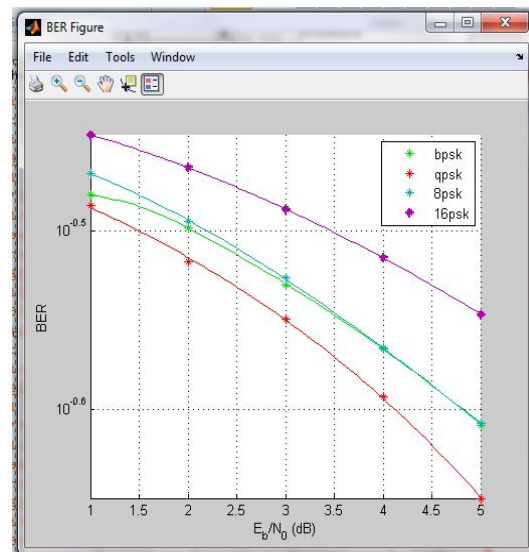


Fig 10:BER for LDPC Model

E. COMPARISON OF VARIOUS CODES

The comparison of various codes is as shown in figure

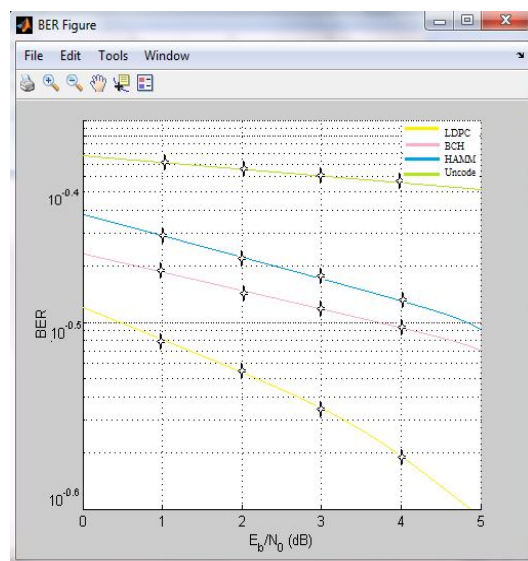


Fig 6: Comparison of various codes

IV. CONCLUSION

In this paper a computer simulation using Matlab has been created by making model which allows the simultaneous analysis of various block code schemes namely, LDPC, Hamming and BCH Codes. The different models were run for 100 frames. Model was designed for better performance and accuracy. The results carry out a comparison of error rate performance of the coding schemes. The various computer based simulation model have been created and their results have been plotted on the graphs of BER vs E_b/N_0 . These result shows that LDPC seem to have better performance then all other block codes. BCH is the extension to the HAMMING code so the performance of BCH is better then HAMMING. It is seen that for smaller value of E_b/N_0 the BCH is having better results and HAMMING give better results for higher value. In some cases the results of HAMMING and BCH overlaps or appear to be closer to each other. On the basis of the results obtained in the present simulation based study, it can be concluded that the LDPC coding scheme is very much effective for retrieval of transmitted data in noisy transmitting medium compared to BCH Hamming and without coding scheme. Though the BCH and Hamming coding scheme provides a definite error correcting capability, the complexity of this code increases as the code length is increased. Further, for a very large code length BCH coding scheme becomes

impractical. LDPC codes provides the best decoding performance.

FUTURE WORK

Some suggestion for future work are as follows:

- I. In LDPC code use different decoding techniques and analyzing their error correction capabilities.
- II. With LDPC, modifying the interleaver and analyzing the performance of the codes with different code rates.
- III. Modifying the frame size to analyze the effect of frame size on block codes.
- IV. Modifying the channel type from AWGN Channel to Rayleigh channel and analyzing the error performance of the Channel coding schemes.

Additionally other coding schemes can also be compared using this simulation setup. On a more complex level multiple coding schemes can be used to determine better error correction capabilities codes.

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